

A large, abstract network graph composed of numerous small, blue, semi-transparent dots connected by thin, light-blue lines. The graph forms a complex, organic shape that tapers towards the right side of the slide.

# Striding Towards Multidimensional Place and Social Space

**Zachary Roman Ph.D.**

Department of Psychology  
University of Zurich

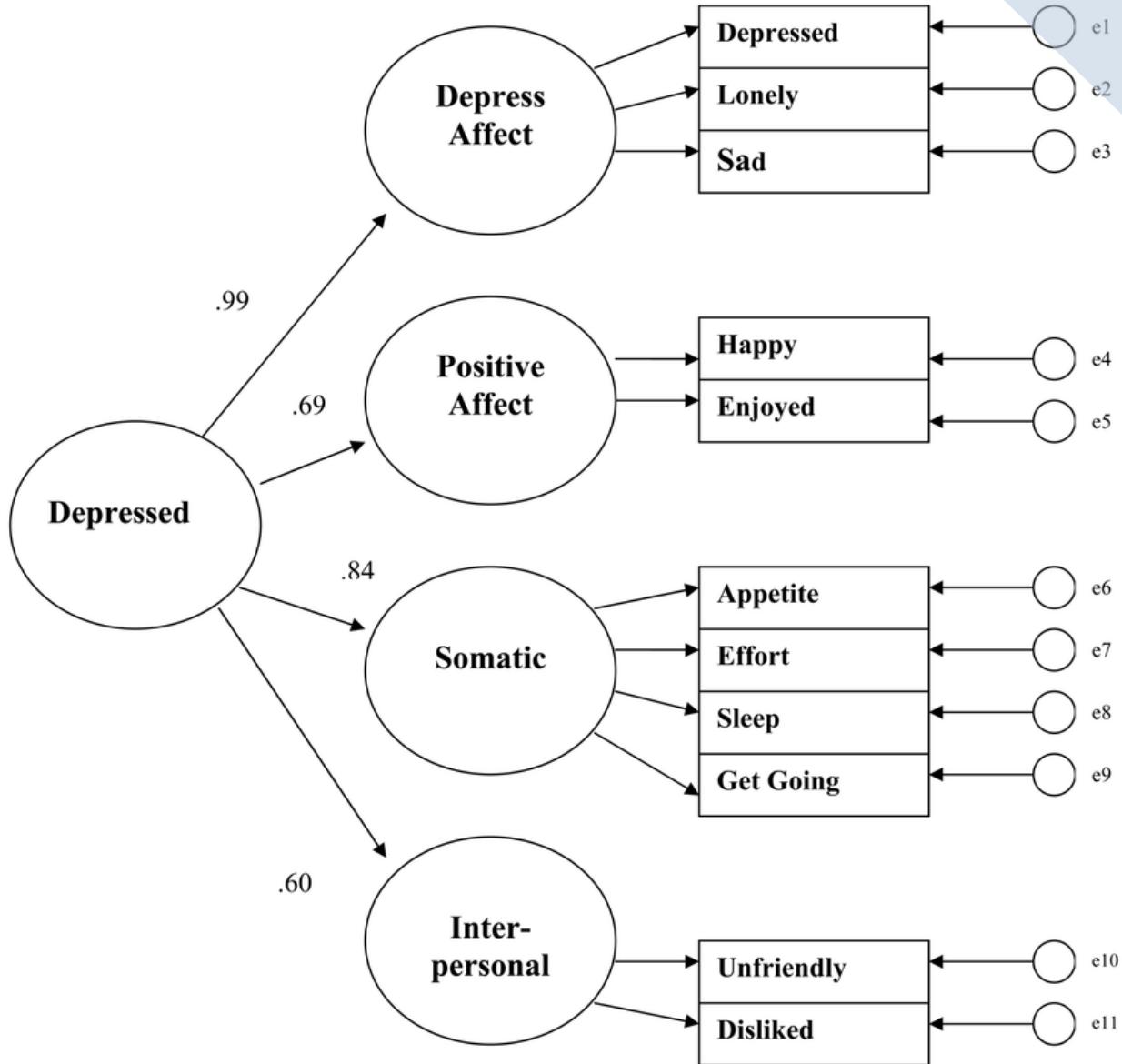
# Personal Background



- 2023 - Current Post-doc Informatics  
Social Computing Group  
University of Zurich
- 2020 - Current Post-doc Psychology  
Quantitative Methods of Intervention & Evaluation  
University of Zurich
- 2019 Ph.D. Quantitative Psychology  
Minor in Computer Science  
University of Kansas
- 2016 M.S. Quantitative Psychology  
Illinois State University
- 2014 B.A. Psychology  
Ohio University

# Latent Variable Models

- Best practice
- Multivariate constructs
- Widely used



# Latent Variable Models

- Best practice
- Multivariate constructs
- Widely used

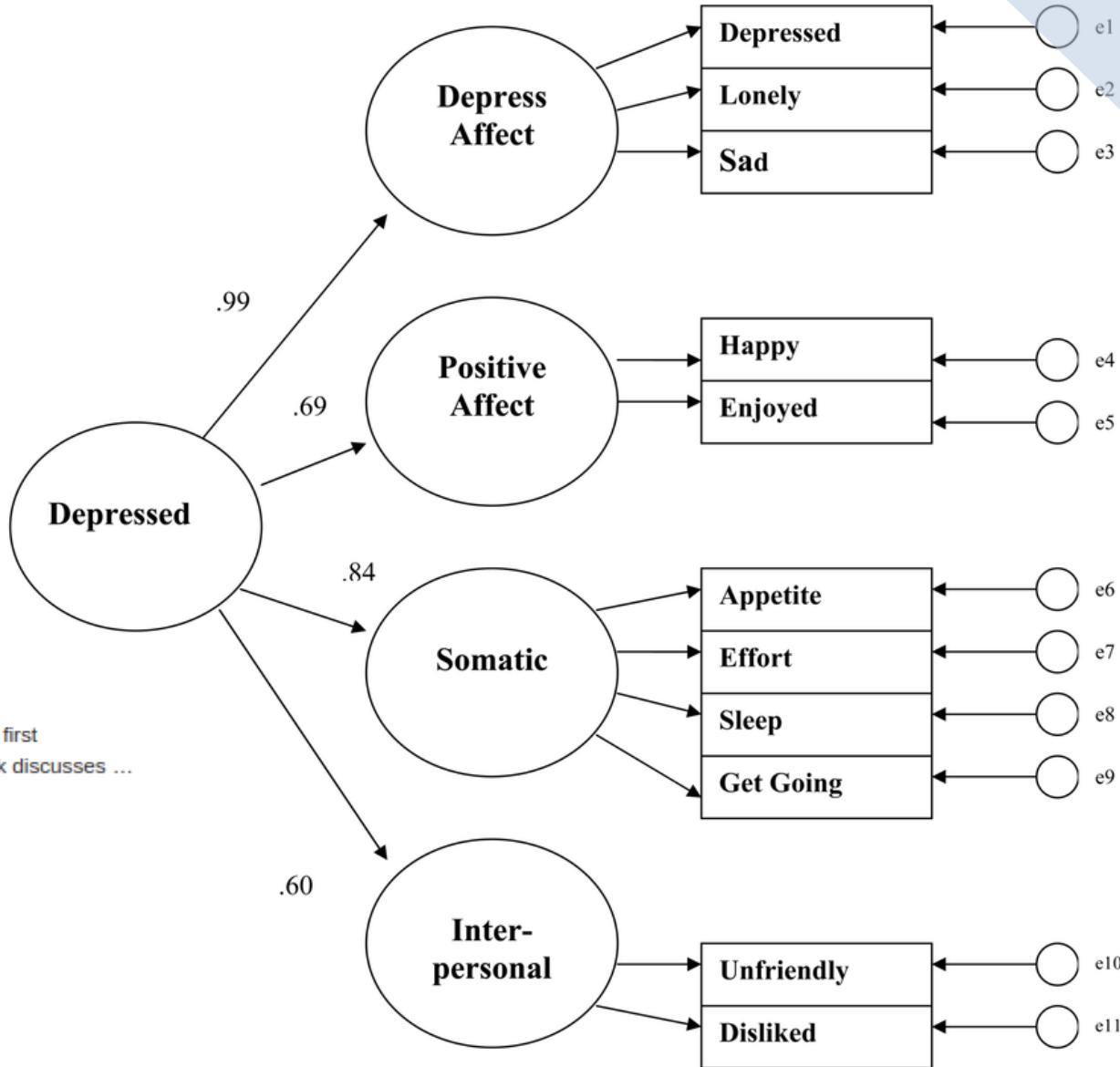
[book] Structural equations with latent variables

[KA Bollen - 1989 - books.google.com](#)

Analysis of Ordinal Categorical Data Alan Agresti Statistical Science Now has its first coordinated manual of methods for analyzing ordered categorical data. This book discusses ...

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- Notable Limitation
  - Dependence

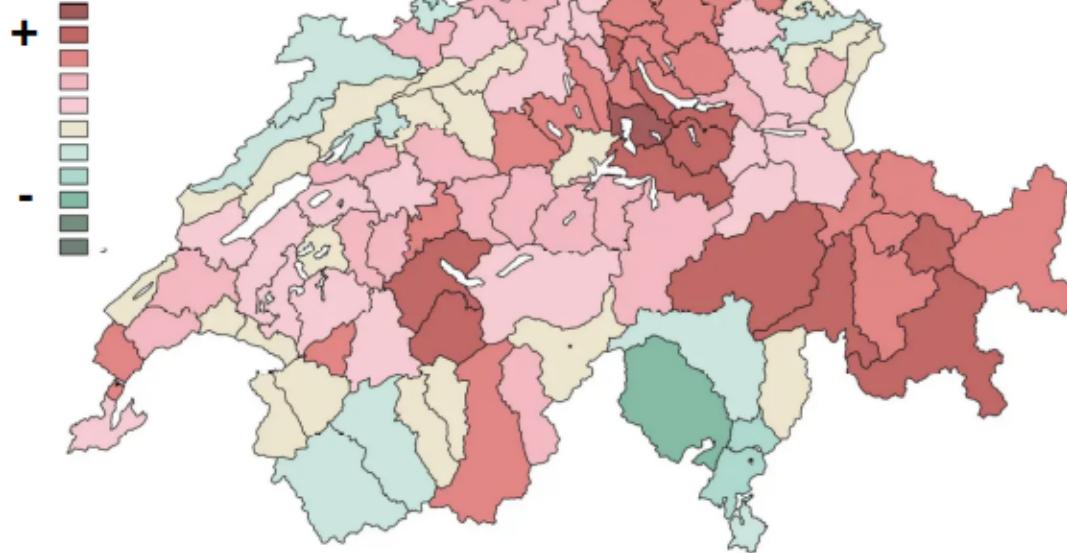


# Spatial & Social Dependence

## Spatial:

- Observations **physically closer** are more similar on a construct

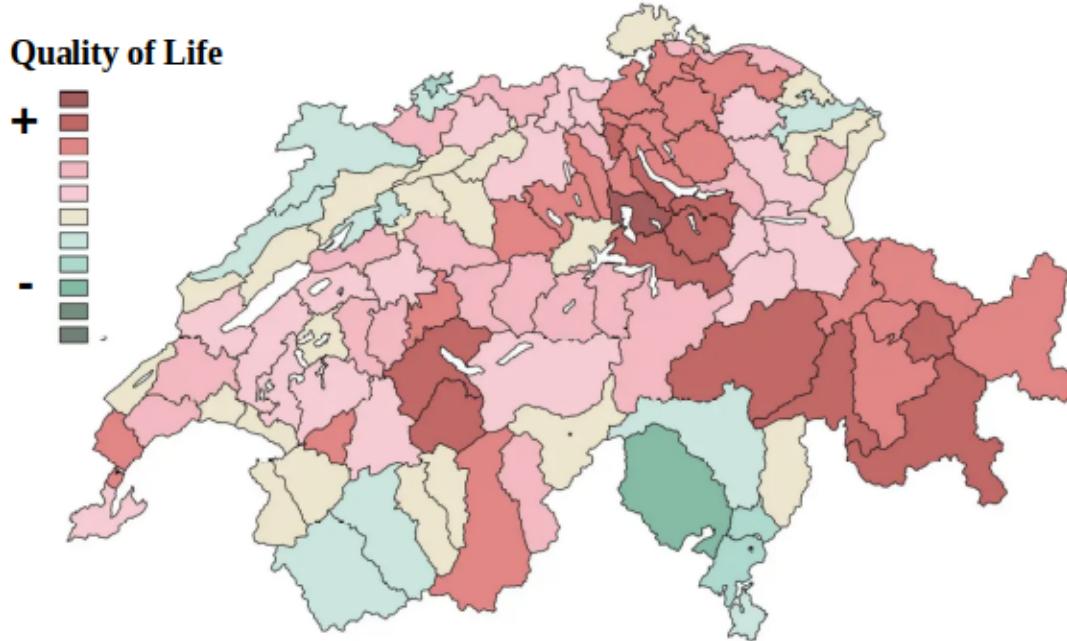
Quality of Life



# Spatial & Social Dependence

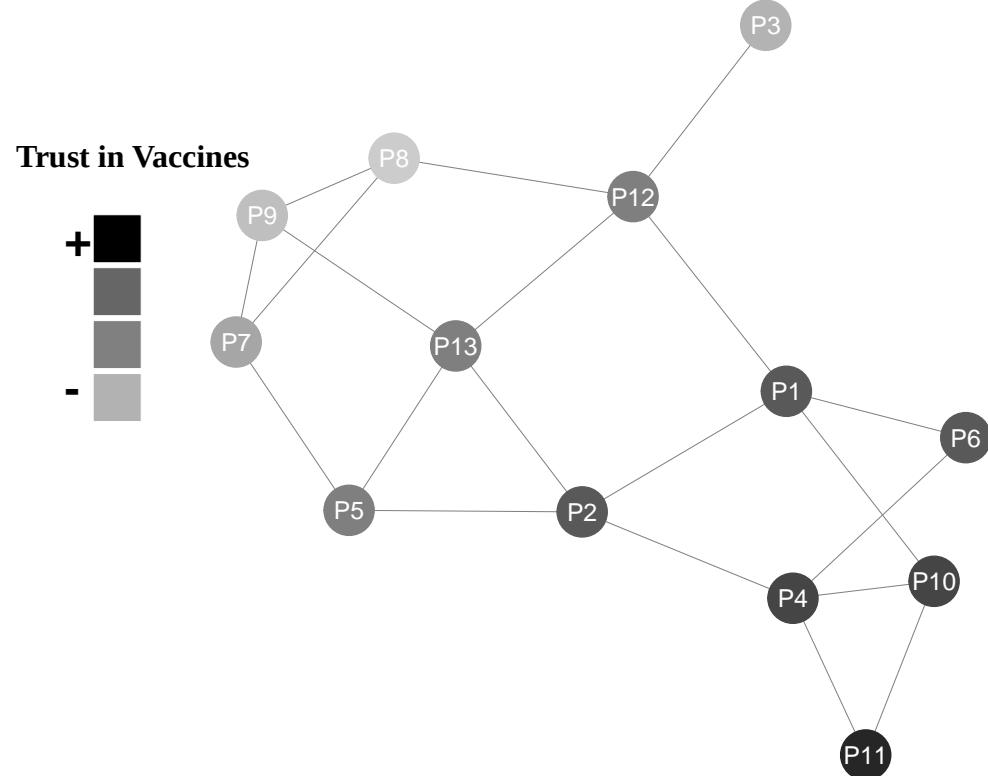
## Spatial:

- Observations **physically closer** are more similar on a construct

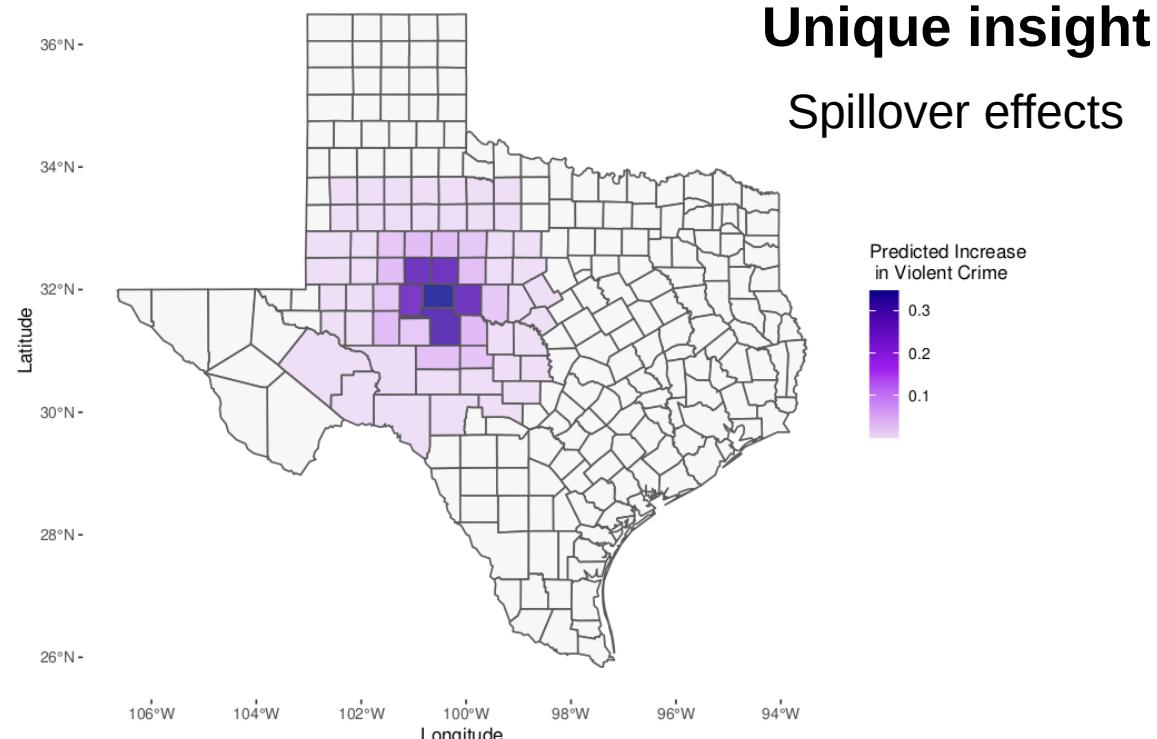


## Social:

- Observations **socially closer** are more similar on a construct



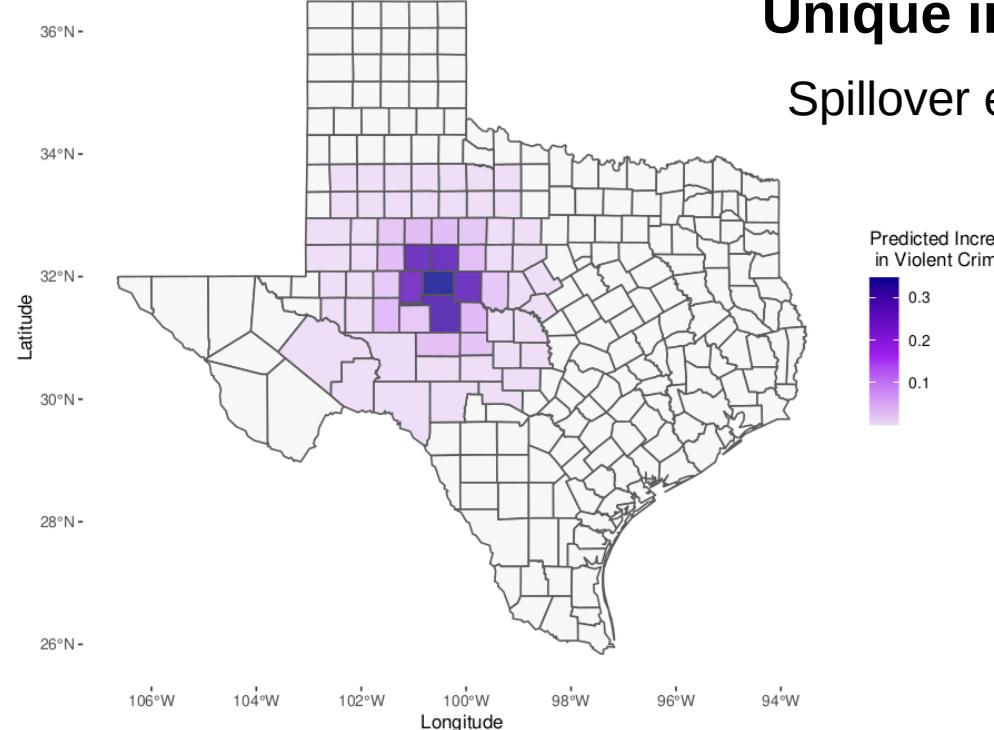
# Modeling Spatial & Social Dependence



Example from:

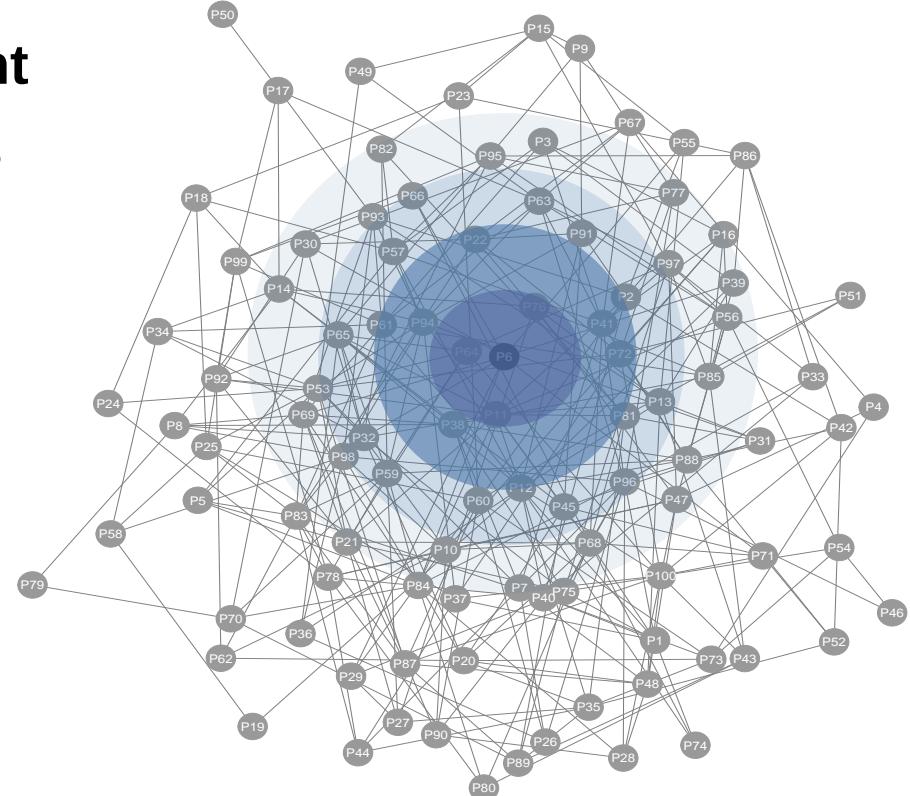
Roman, Z. J. & Brandt, H. (2021). A latent auto-regressive approach for Bayesian structural equation modeling of spatially or socially dependent data. *Multivariate Behavioral Research*, 1-25.

# Modeling Spatial & Social Dependence



Unique insight

Spillover effects



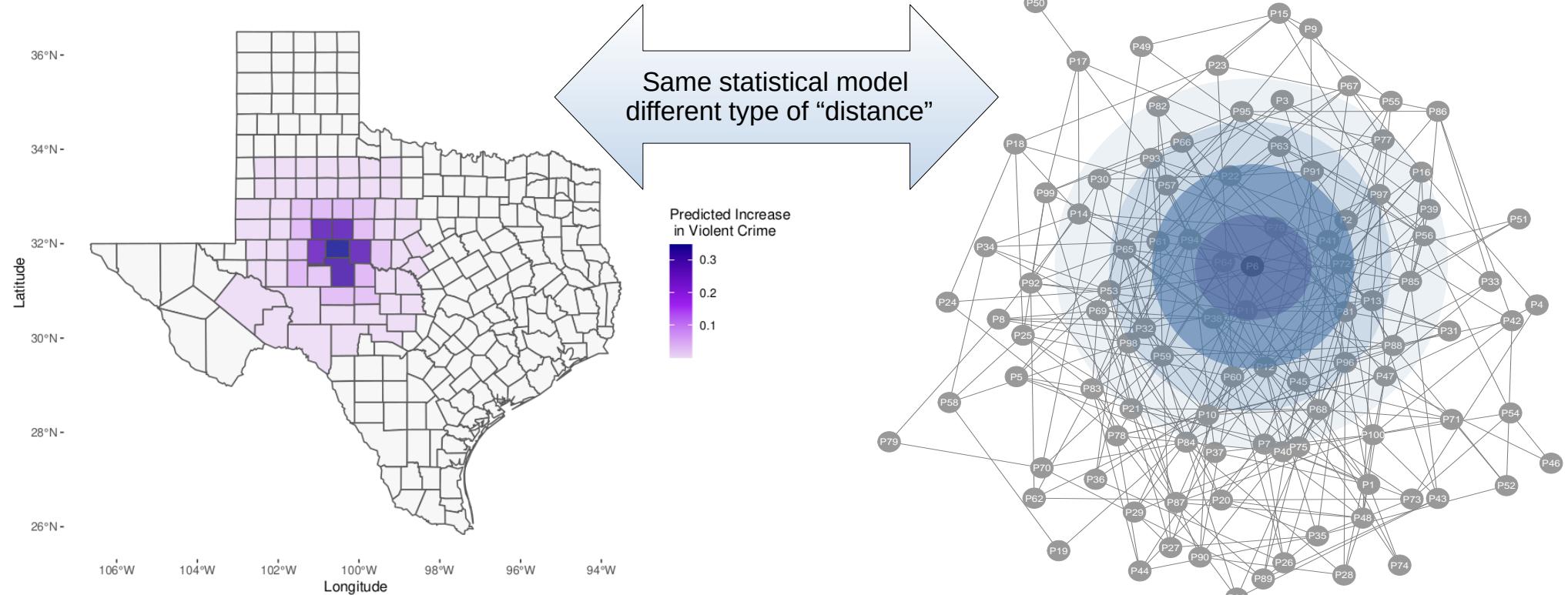
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Example adapted from:

Roman, Z. J. (2021). Spatial and Social Network Auto-regressive Structural Equation Modeling [Conference oral presentation]. 15th Conference of Fachgruppe Methoden und Evaluation (FGME) annual meeting, University of Mannheim.

# Modeling Spatial & Social Dependence



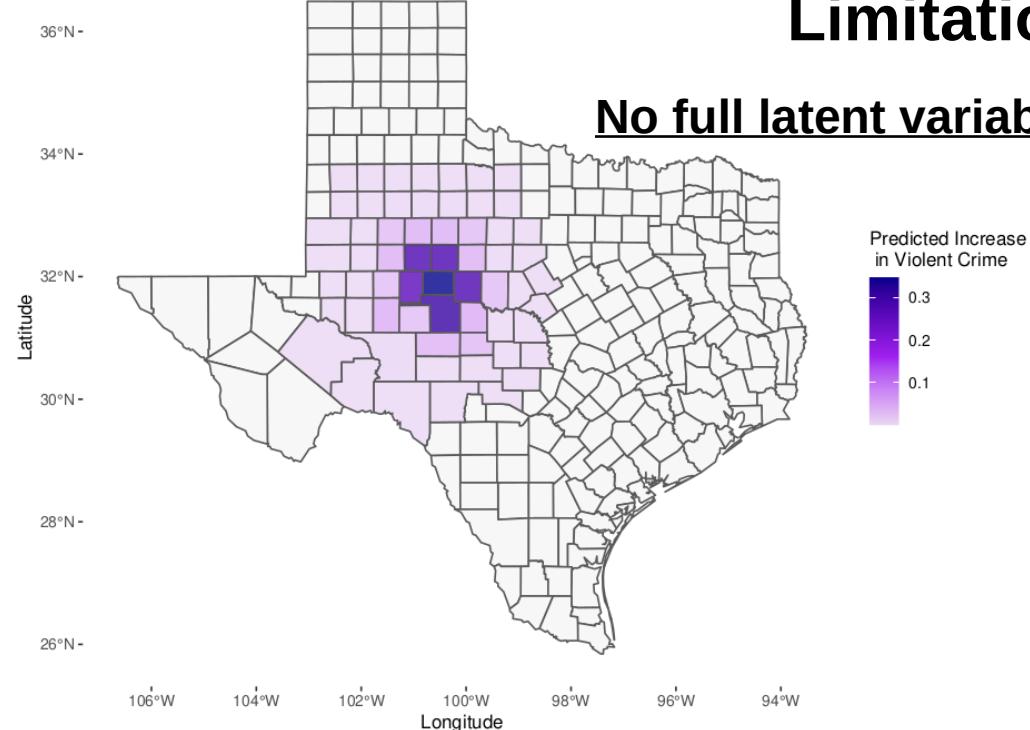
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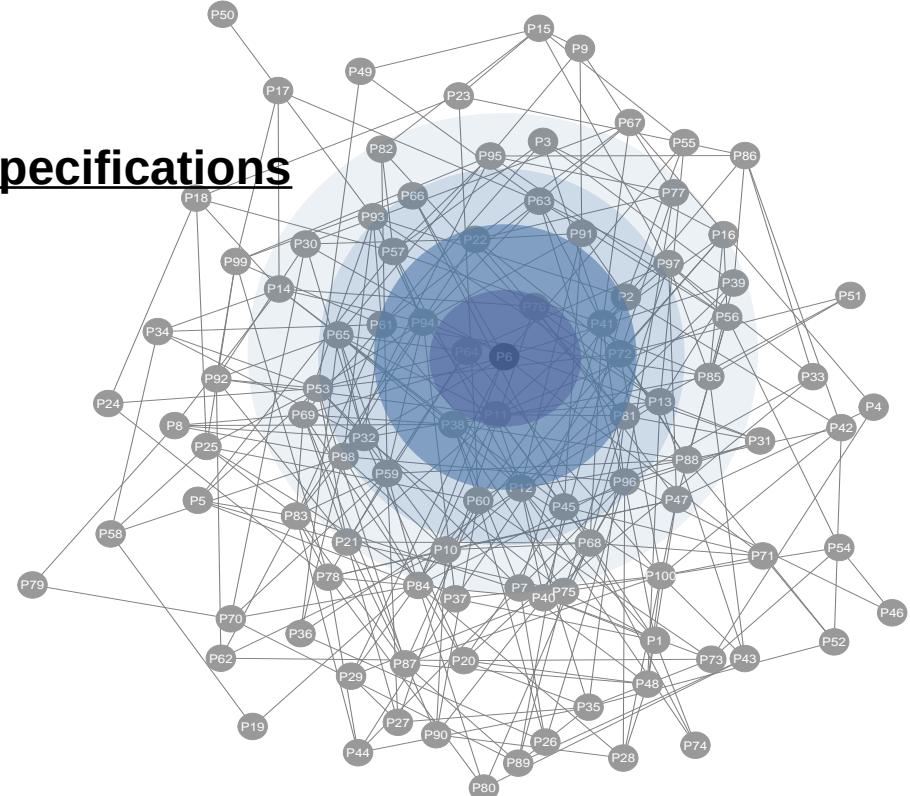
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# Modeling Spatial & Social Dependence



## Limitation

No full latent variable specifications



Example from:

Roman, Z. J. & Brandt, H. (2021). A latent auto-regressive approach for Bayesian structural equation modeling of spatially or socially dependent data. *Multivariate Behavioral Research*, 1-25.

Example adapted from:

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# Project Overview

## Goals

Create spatial & social dependence latent variable modeling framework

Create open source software package

## Milestone

## Completion Goal

I

Develop observed multi-group model

II

Develop unobserved multi-group model  
(Latent classification)

III

Develop clustered group multi-level model

IV

Develop Longitudinal multi-level model

V

Create Open source software (R-package)

VI

Author framework tutorial paper

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## Completion Goal

Month 8

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Month 16

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Month 16

Month 24

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## Completion Goal

Month 8

Month 16

Month 24

Month 32

-Model developments were selected to maximize scientific impact and accessibility

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Month 16

Month 24

Month 32

Month 40

Reproducible Research



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Month 8

Month 16

Month 24

Month 32

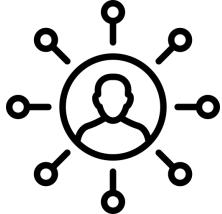
Month 40

Month 48

Reproducible Research



# Network of Project Collaborators



- Methodological**
- Application**
- Software**

**Prof. Arkady Konovalov**  
University of Birmingham - UK

**Prof. Holger Brandt**  
**Prof. Augustin Kelava**  
University of Tuebingen - DE

**Prof. Carolin Strobl**  
**Prof. Birgit Kleim**  
**Prof. Aniko Hannak**  
**Prof. Urte Scholz**  
**Prof. Nicolas Langer**  
University of Zurich - CH

**Prof. Jörg Müller**  
Open University of Catalonia - ES



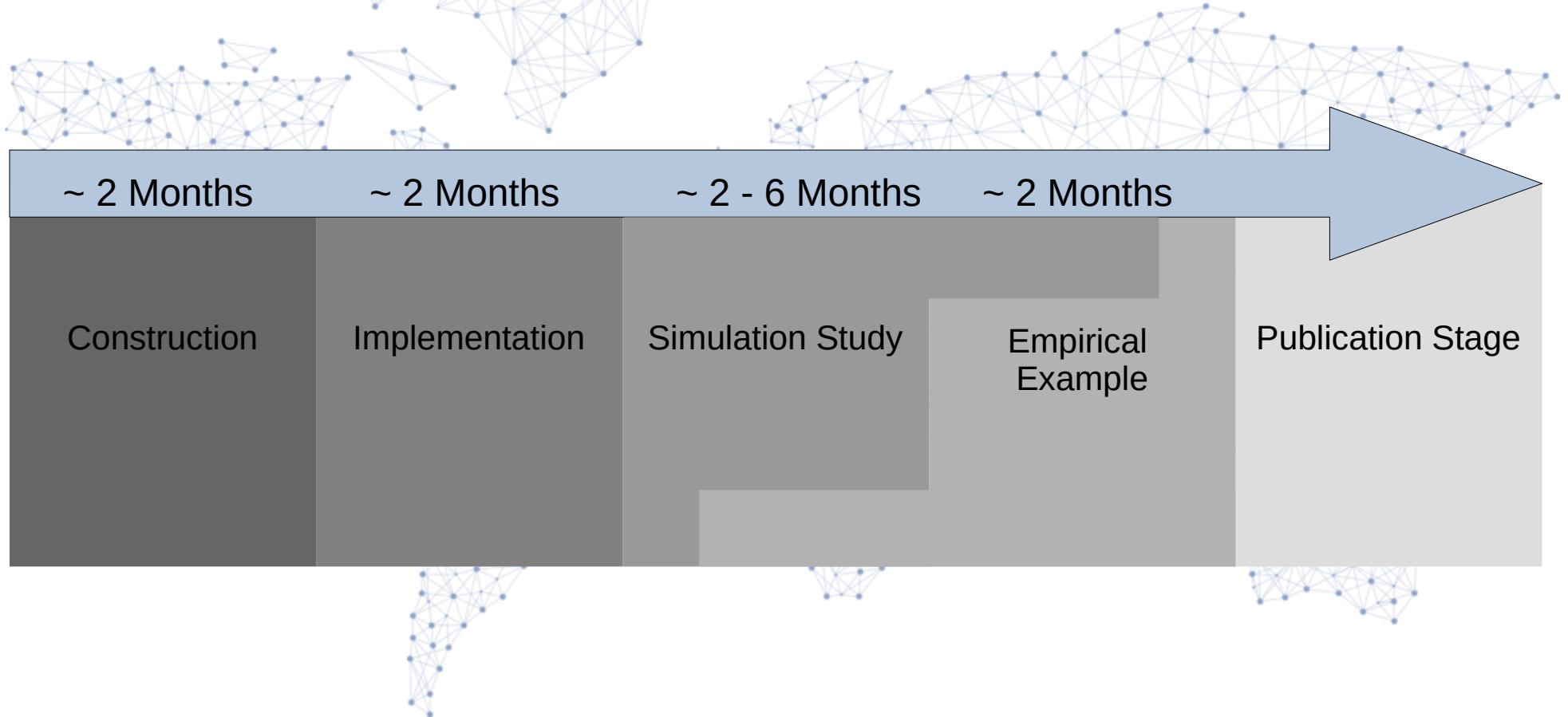
**Prof. Ed Merkle**  
University of Missouri

**Prof. Christian Crandall**  
University of Kansas

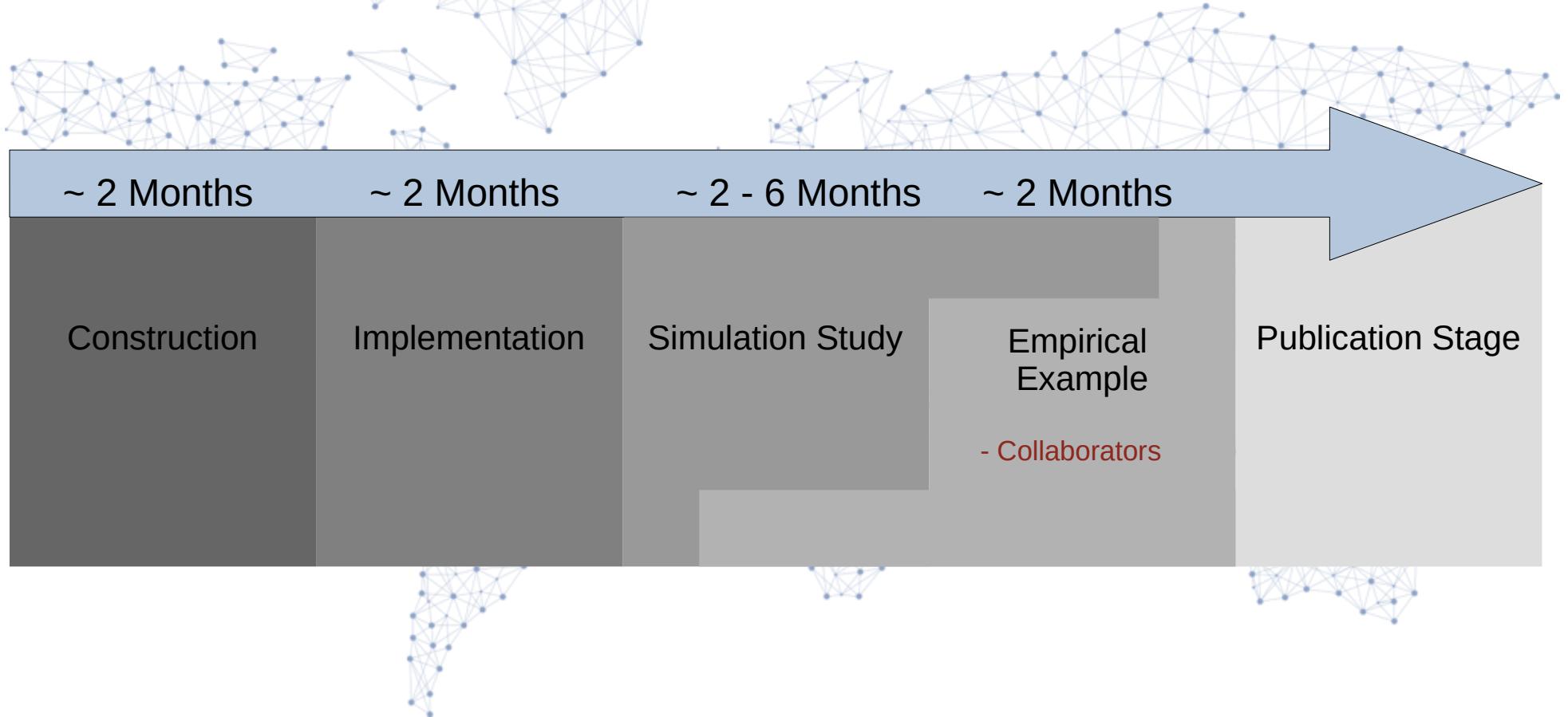
**Prof. Dan Bauer**  
**Dr. Chris Urban**  
University of North Carolina



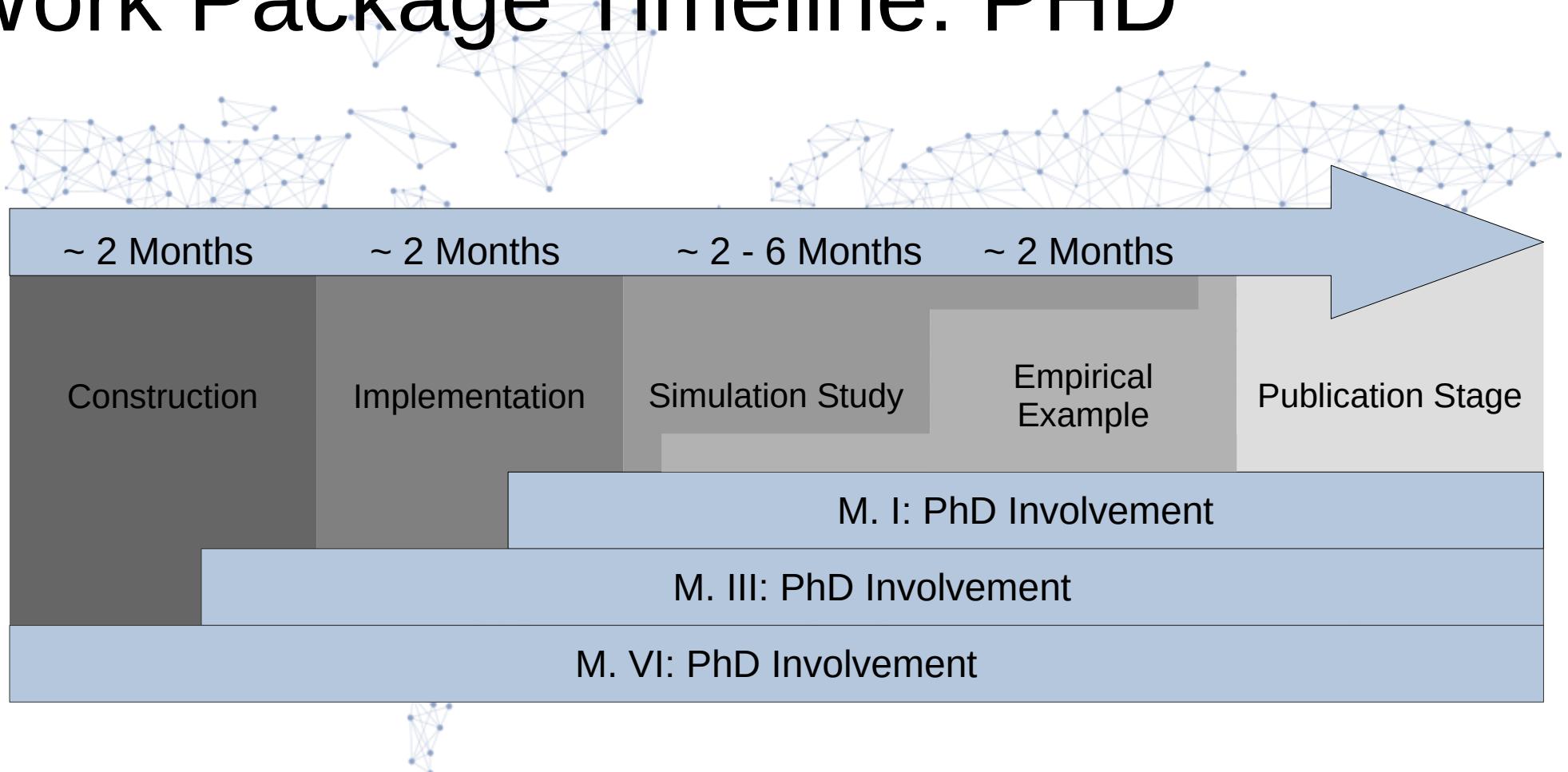
# Work Package Timeline



# Work Package Timeline



# Work Package Timeline: PHD



# Project Outcome

- Full latent variable dependence modeling framework
  - Old theories new perspectives
  - New theories
  - Novel and unique insights
    - Combined approach is more than the sum of its parts

# Beyond Ambizione

- Impact to many disciplines
  - Psychology, sociology, political science, economics, public policy, epidemiology, biology etc.

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  - Neuropsychology

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- Many more directions
  - Methodological
  - Neuropsychology
- Professorship
  - Eccellenza
  - Tenure Track

# Thank You!

## Content related publications:

**Roman, Z. J.**, Schmidt, P., Miller, J. M., & Brandt, H. (2023). Identifying dynamic shifts to non-compliant behavior in questionnaire responses; A novel approach and experimental validation. *[Pre-print available, under review]*

**Roman, Z. J.**, Brandt, H., & Miller, J. M. (2022). Automated bot detection using Bayesian latent class models in online surveys. *Frontiers in Psychology*, 1947.

**Roman, Z. J.** & Brandt, H. (2021). A latent auto-regressive approach for Bayesian structural equation modeling of spatially or socially dependent data. *Multivariate Behavioral Research*, 1-25.

**Roman, Z. J.** (2019). Auto-regressive latent variable modeling: A general framework for Bayesian spatial structural equation models (Doctoral dissertation, University of Kansas).

# Appendix



# Milestone I: Multi-group Model

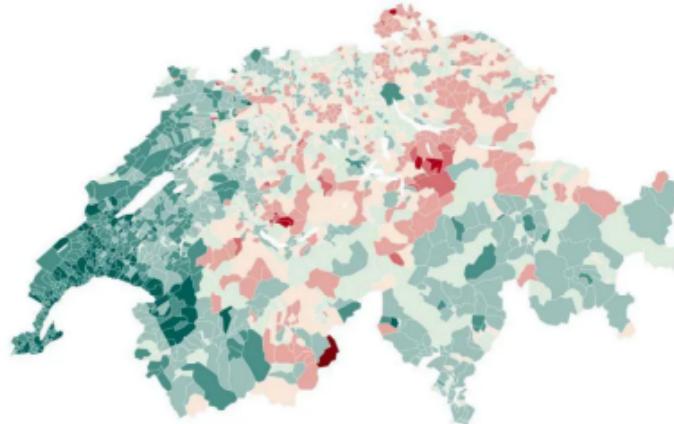
Bayesian auto-regressive dependence multi-group structural equation model

- Full latent variables
- Spillover interactions compared across groups
- Experimental & quasi-experimental applications

Quality of Life

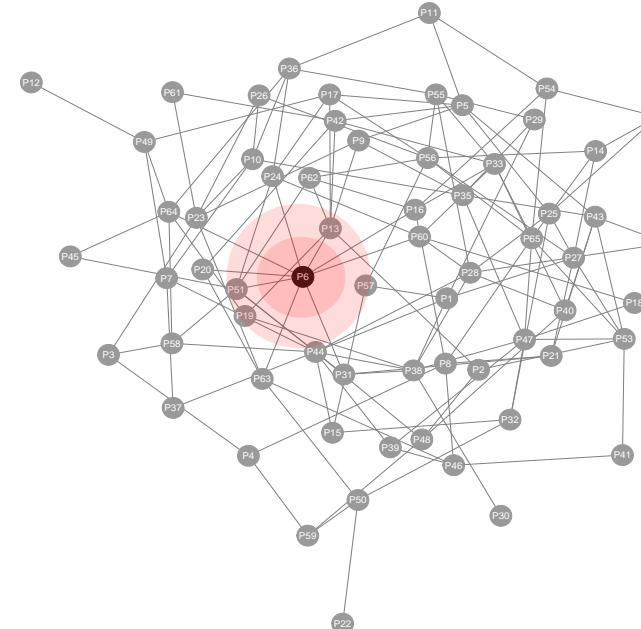
Romande

German

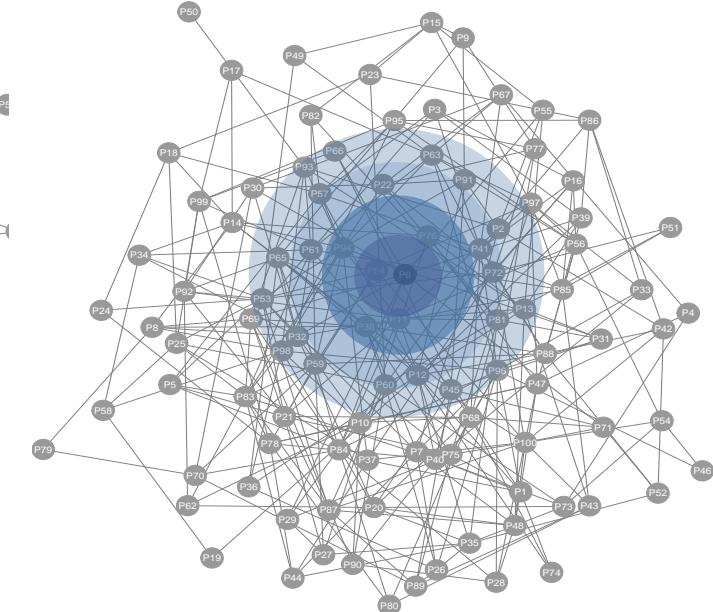


Misinformation

Political Leftists



Political Rightist



# Work Package Timeline: Data

## Empirical Example

- Gender Diversity Impact Study (GEDII)
  - Prof. Jörg Müller
- Temporal Dynamics of Health Behavior Change\*
  - Prof. Urte Scholz
- Optimising Outcomes in Psychotherapy for Anxiety Disorders (OPTIMX) \*\*
  - Prof. Birgit Kleim
- Social Media Scraping
  - Prof. Aniko Hannak

\* SNF grant number 197471

\*\* SNF grant number 169827

A large, abstract network graph composed of numerous small, semi-transparent blue dots connected by thin lines, forming a complex web-like structure that spans the entire background.

# Bayesian Auto-regressive Dependence Latent Variable Modeling Technical Details

# Spatial Auto-regression

## Traditional Linear Regression

$$y_i = \alpha + x\beta_1 + \epsilon_i, \quad \epsilon_i \sim N(0, \sigma I_N) \quad (1)$$

## Spatial Auto-Regression (SAR)

$$y_i = \underbrace{\rho \mathbf{W} y_i}_{\text{Spatial Lag}} + \alpha + x\beta_1 + \epsilon_i, \quad \epsilon_i \sim N(0, \sigma I_N) \quad (2)$$

Where:

- $\rho$  summarizes the spatial auto-correlation in the dependent variable.<sup>a</sup>
- $\mathbf{W}$  is an  $N \times N$  matrix summarizing the dependence of the cases

---

<sup>a</sup>When  $\rho = 0$  traditional regression and spatial regression are equivalent

# BARDSEM (Roman & Brandt, 2021)

## Measurement Model

$$y_j = \tau_{yj} + \lambda_{yj}\eta + \epsilon_j, \quad \epsilon_j \sim N(0, \sigma_\epsilon^2) \quad (4)$$

$$x_k = \tau_{xk} + \lambda_{xk}\xi + \delta_k, \quad \delta_k \sim N(0, \sigma_\delta^2) \quad (5)$$

## Structural Model

$$\eta = \alpha + \underbrace{\rho_\eta \mathbf{W}\eta}_{\text{Spatial Lag}} + \gamma_1\xi_1 + \gamma_2\xi_2 + \gamma_3 h(\xi) + \zeta, \quad \zeta \sim N(0, \sigma_\zeta^2) \quad (6)$$

## Error Distributions

- $\epsilon_j \sim N(0, \sigma_{\epsilon j}^2)$ , for  $j = 1 \dots J$
- $\delta_k \sim N(0, \sigma_{\delta k}^2)$ , for  $k = 1 \dots K$
- $\zeta \sim N(0, \sigma_\zeta^2)$

# BARDSEM Priors

## Priors

- $\rho_\eta \sim U[1 - \min(\lambda_W), 1 - \max(\lambda_W)]$
- $\gamma, \lambda, \alpha, \tau \sim N(0, 1)$
- $\sigma_* \sim \text{Cauchy}(0, 2.5)^+$
- $\Phi \sim \text{LK}_j(I_2, 2)$



# Spillover Computation

**Computing**  $\partial_{\eta}/\partial_{\xi}^{p'}$

$$\partial_{\eta}/\partial_{\xi}^{p'} = (\mathbf{I}_n - \rho \mathbf{W})^{-1} \mathbf{I}_n \gamma_p \quad (3)$$

Where:

$p = 1 \dots P$  indicates the respective exogenous latent variable

$\mathbf{I}_n$  is an identity matrix of length  $n$

**Interpreting**  $\partial_{\eta}/\partial_{\xi}^{p'}$

- Cell  $i, j$  of  $\partial_{\eta}/\partial_{\xi}^{p'}$ , provides the anticipated impact of case  $j$  on case  $i$
- Direct interpretation of  $\partial_{\eta}/\partial_{\xi}^{p'}$  is possible but potentially burdensome
- Impact measures summarize the matrix to ease interpretation



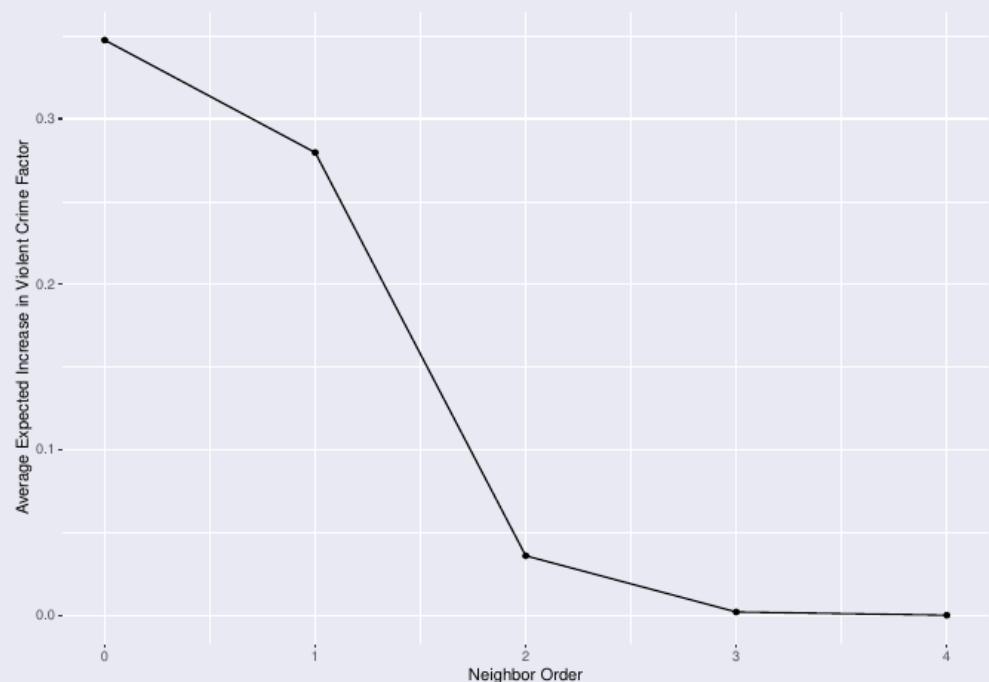
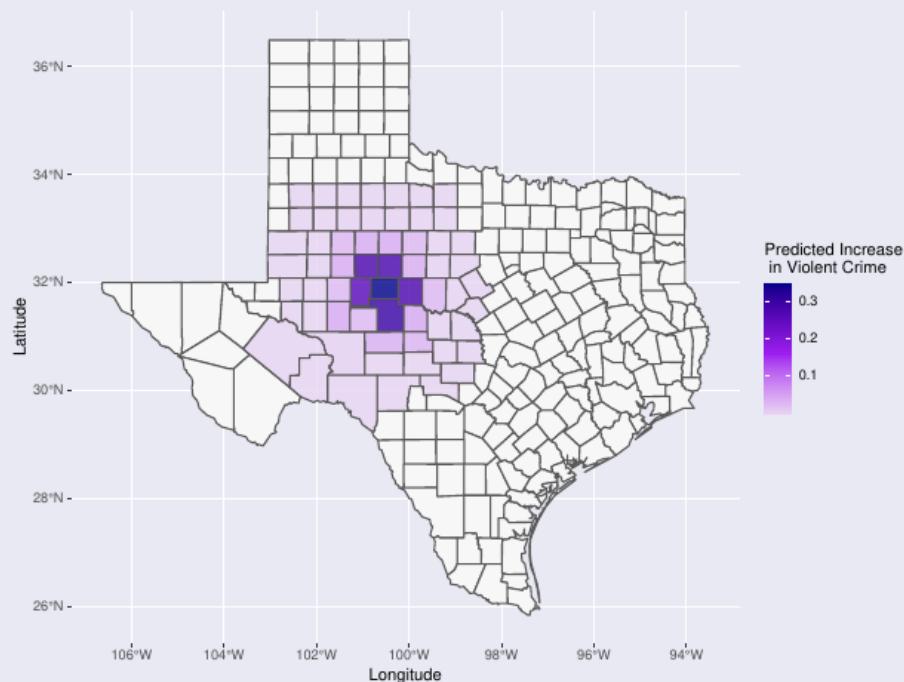
# Summarizing Spillover

Summarize  $\partial \eta / \partial \xi^{p'}$

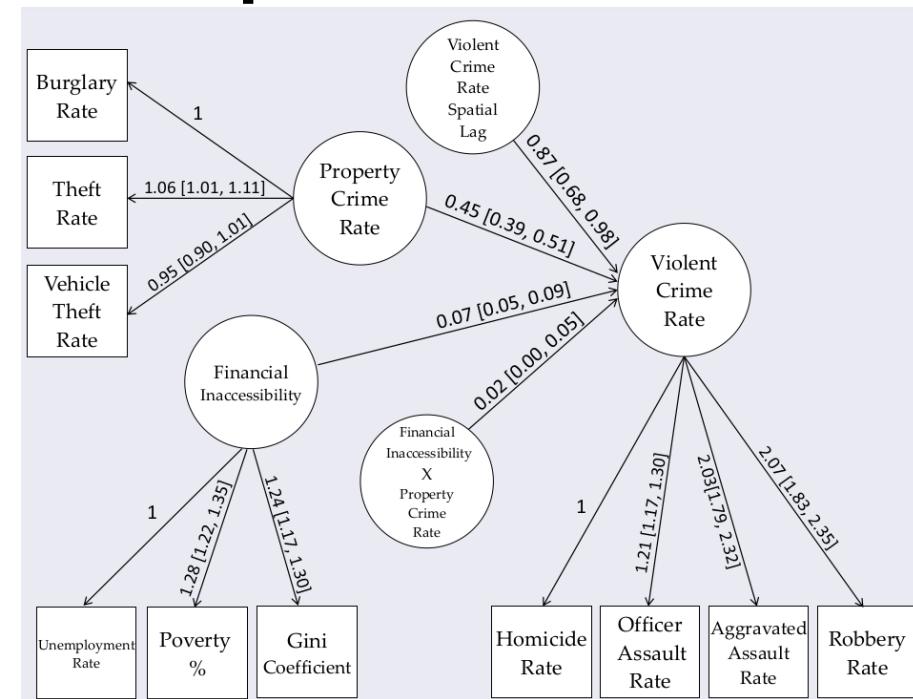
- Direct
  - Mean of diagonal
  - Expected mean change in the outcome of case  $\neq i$  for a 1 unit increase in predictor  $p$  in case  $i$
- Indirect
  - Mean of off diagonal
  - Expected mean change in the outcome of case  $i$  for a 1 unit increase in predictor  $p$  in all  $\neq i$  cases.
- Total
  - Mean of matrix
  - Expected mean change in case  $i$  for a 1 unit increase in all cases (Including case  $i$ )

# Spillover is a nonlinear function over space

## Property Crime Spillover



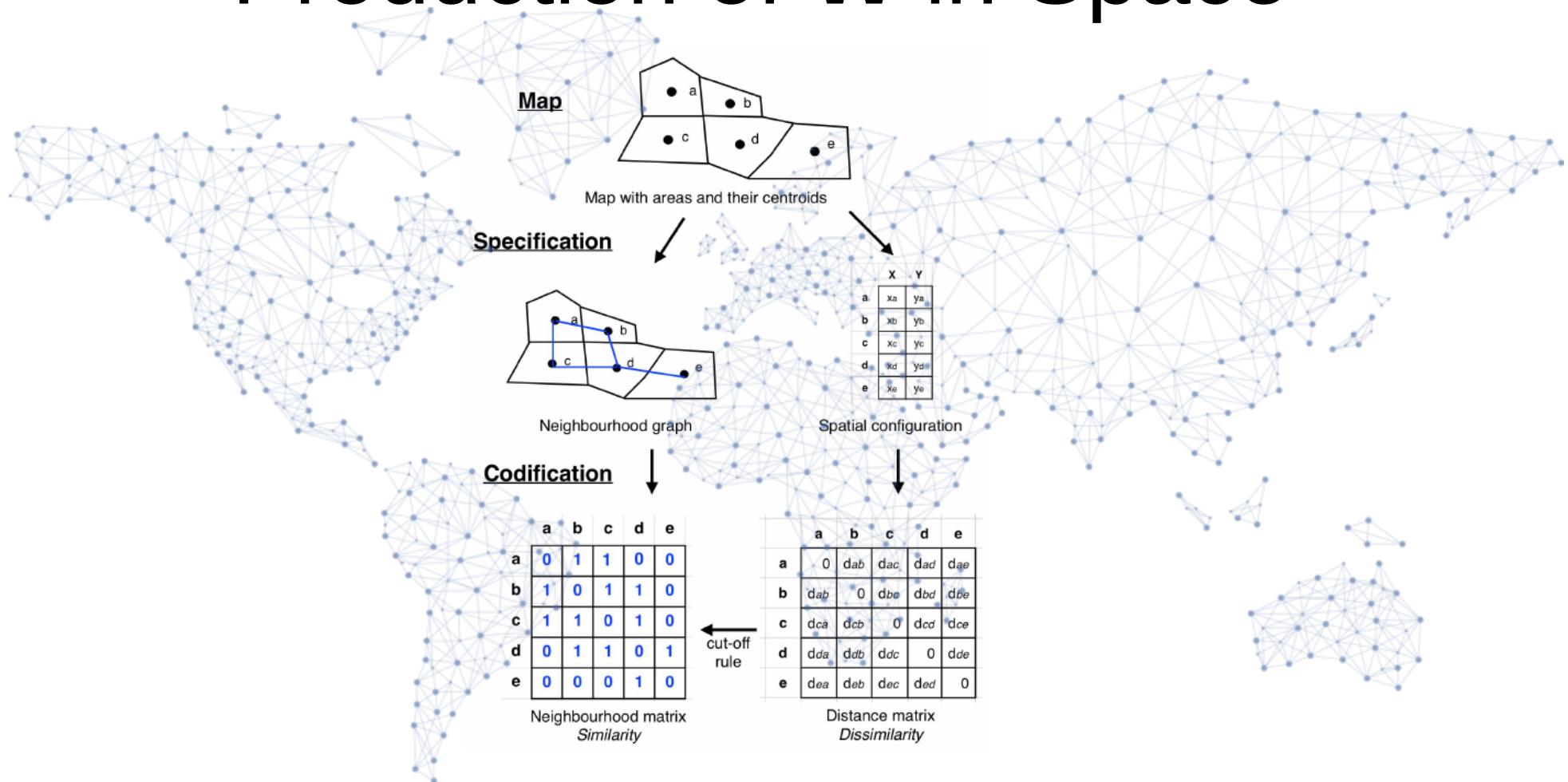
# Spatial Spillover Example: Latent Variables



## Simple Slopes Spillover Effects

	Direct Impact (2.5%, 97.5%)	Indirect Impact (2.5%, 97.5%)	Total Impact (2.5%, 97.5%)
$\gamma_{\text{Property}} \mid \xi_{\text{Fin. Inac.}} = -2$	0.55 (0.47, 0.60)	2.60 (2.22, 2.86)	3.15 (2.69, 3.46)
$\gamma_{\text{Property}} \mid \xi_{\text{Fin. Inac.}} = -1$	0.58 (0.50, 0.64)	2.73 (2.35, 3.05)	3.31 (2.85, 3.69)
$\gamma_{\text{Property}} \mid \xi_{\text{Fin. Inac.}} = 0$	0.60 (0.52, 0.68)	2.86 (2.48, 3.24)	3.46 (3.01, 3.92)
$\gamma_{\text{Property}} \mid \xi_{\text{Fin. Inac.}} = 1$	0.63 (0.55, 0.72)	2.98 (2.60, 3.43)	3.62 (3.15, 4.15)
$\gamma_{\text{Property}} \mid \xi_{\text{Fin. Inac.}} = 2$	0.66 (0.58, 0.76)	3.11 (2.73, 3.62)	3.77 (3.31, 4.38)

# Production of W in Space





# Simulation Study Designs

# Milestone I

- Conditions follow those of Roman & Brandt (2021)
- Simulation Conditions
  - # of observed groups
  - Magnitude of connectivity matrix  $\mathbf{W}$ 
    - High, medium, low
  - Connectivity structure
    - Social or spatial representation
  - Sample size
    - High, medium, low, very low
  - Effect sizes
    - Auto-regressive Coef.
    - Difference in auto-reg. Coef. By group
  - Complexity of Measurement model
    - 3 – 10 observed items per indicator
- Measuring model performance
  - Bias
  - Coverage + Error Rates
  - Convergence

# Milestone II

- Conditions follow those of Roman & Brandt (2021)
- Simulation Conditions
  - **# of unobserved groups**
  - Magnitude of connectivity matrix  $\mathbf{W}$ 
    - High, medium, low
  - Connectivity structure
    - Social or spatial representation
  - Sample size
    - High, medium, low, very low
  - Effect sizes
    - Auto-regressive Coef.
    - Difference in auto-reg. Coef. By group
  - Complexity of Measurement model
    - 3 – 10 observed items per indicator
- Measuring model performance
  - Bias
  - Coverage + Error Rates
  - Convergence

# Milestone III

- Conditions follow those of Roman & Brandt (2021)
- Simulation Conditions
  - # of Level 2 clusters
  - Magnitude of connectivity matrix  $\mathbf{W}$ 
    - High, medium, low
  - Connectivity structure
    - Social or spatial representation
  - Sample size
    - High, medium, low, very low
  - Effect sizes
    - Auto-regressive Coef.
    - Difference in auto-reg. Coef. By group
  - Complexity of Measurement model
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  - Coverage + Error Rates
  - Convergence

# Milestone IV

- Conditions follow those of Roman & Brandt (2021)
- Simulation Conditions
  - # of measurement occasions
  - Magnitude of connectivity matrix  $\mathbf{W}$ 
    - High, medium, low
  - Connectivity structure
    - Social or spatial representation
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# R packages

## **lavaan: An R package for structural equation modeling**

[Y Rosseel - Journal of statistical software, 2012 - jstatsoft.org](#)

... paper describes **package lavaan**, a **package** for structural equation modeling implemented in the R system for statistical computing (R Development Core Team 2012). The **package** is ...

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## **blavaan: Bayesian structural equation models via parameter expansion**

EC Merkle, Y Rosseel

Journal of Statistical Software 85 (4), 1-30

[PDF] [jstatsoft.org](#)

243

2018

- Accessible user experience
- Highly citable tools
- Guidance in documentation
- Working examples